=

=

7 ci fgY⁻Cj Yfj]Yk

GHJZT7cbHJWh78YHJ]`g

7 cbj Ybcfg

BUa Y	9a U]`	5j U]`UV]`]m	@cWUhjcb	D∖cbY
DYma Ub	dYmaUb4 i bgk "YXi "Ui			
A cgHJ[\]a]				

8Ya cbghfUhcfg

BUa Y	9a U]`	5j U]`UV]`]m	@cWUhjcb	D∖cbY
: UhYa Y\`Gc`Y]a Ub]	Z'gc`Y]a Ub]4 i bgk "YXi "Ui			

GWX.cc``7cbHJWhi=bZcfaUh]cb

GW&cc``cZA]bYfU`g`UbX`9bYf[mFYgcifWYg C`X`AU]b`6i]`X]b[ž`@YjY``%z`%) - `fP%)Ł IBGK `GM8B9MBGK`&\$)&5IGHF5@=5

<u>9b[]bYYf]b[Gh XYbhGYfj]Wg</u>

9. a YfY"hYUW\]b[4 i bgk "YXi "Ui

K . <u>k k k "Yb[]bYYf]b["i bgk "YXi "Ui #a]bYfU`g!YbYf[mfYgci fW/g</u>

7ci fgY[·]8YHJ]`g

7 fYX]hDc]bhg***

Gi a a UfmcZhXY7ci fgY

=bfcXi Wijcb'hc'F YgYfj c]f'9b[]bYYf]b["'F YgYfj c]f'8YgWf]dh]cb"' < mXfcgHJh]WdfYggi fY'UbX'[Ych\Yfa U' [fUX]Ybhg"'Dcfcg]hmidYfa YUV]']hmfY'Uh]cbg\]dg'UbX'fcW_'a]Wfcghfi Wi fYg"'J c'i a Yhf]WUbX']b]h]U` \mXfcWJfVcb'j c'i a Y"': `i]X'GHJh]Wg": `i]X'Zck gž'Ua]bUf'UbX'hi fVi `YbhZck g"'6ci bXUfm`UmYfg":: `ck ']b d]dYgž/Z]Wi]cb']b'd]dYž'9i `Yf'UbX'6Yfbci ``]fig'Yei Uh]cb"'5b[i `Uf'a ca Ybhi a 'Yei Uh]cb"'GhYUXmZck 'YbYf[m Yei Uh]cb"'A]bcf`cggYg":: `ck 'cj Yf'gi fZJVWg"'GhYUXmgHJhY']bW]bYX'Zck 'UbX'dfYggi fY'dchYbh]U`"GhYUXm gHJhY'fUX]U``Zck ":: `ck ']b'gYf]Yg'UbX']b'dUfU``Y'"J Yff]WU`'k Y``a cXY``UbX'g_]b'YZYWf

7cifgY`@YUfb]b[`CihWcaYg

- %" I bXYfgHUbX'UbX'Udd`mZ bXUa YbHU`'H\Ycf]Yg'UbX'WcbWYdhg'hc'gc`j Y'a UbmifYgYfj c]f'Yb[]bYYf]b[dfcV`Ya gž'Y"["`]b]h]U``\mXfcWUfVcb']b'd`UVW'ž'VUg]WfcW_'UbX'Zi]X'dfcdYfh]Ygž`\mXfcgHUh]WdfYggi fY X]gHf]Vi h]cbž'k UHYf`]bZi I 'UbX'g]b[`Y'd\UgY'Zi]X'Zck
- &" 7 f]h]WU``mUbU`mgY`h\Y`i bXYf`m]b[`h\Ycf]YgžWcbWYdhgžUggi a dh]cbg`UbX`Uf[i a Ybhg`WcbWYfb]b[`Zi]X Zck``i bXYf`X]ZYfYbhfYgYfj c]f`WcbX]h]cbg

HYUWX]b[GhfUhY[]Yg

D`YUgY`fYZYf`hc`h\Y`]bZcfaUh]cb`]b`AccX`Y

5ggYgga Ybh

5ggYgga YbhHUg_g

5ggYgga Ybh'HJg_	K Y][\h	8iY'8UHY	GhiXYbhi@YUfb]b[CihWcaYgʻ5ggYggYX
A]XhYfa 'Ei]n'%'	%\$I	Bch5dd`]WUV`Y	%ž`&
A]XhYfa 'Ei]n'&'	%) I	Bch5dd`]WUV`Y	%ž`&
A]XhYfa 'Ei]n'' '	%) I	Bch5dd`]WUV`Y	%ž`&
5gg][ba Ybhg	%\$I	Bch5dd`]WUV`Y	%ž`&
:]bU``9I Ua `)\$I	Bch5dd`]WUV`Y	%ž`&

5ggYgga Ybh8YHJ]`g

5ggYgga Ybh% A]XhYfa Ei]n%

GHJfh'XUHY. `\$' #\$' #&\$&%`%&.\$\$`DA

 $8\,YHJ$ `g.A]XhYfa 'Ei]n'%

5ggYgga Ybh& A]XhYfa Ei]n &

GHJfh'XUHY. '%+#\$' #&\$&%'%&.\$\$ DA

8YHJ]`g.A]XHYfa 'Ei]n'&

5ggYgga Ybh' A]XhYfa Ei]n'

GHJfh'XUhY. *\$+#\$(#&\$&%'%&.\$\$*DA

8YHJ]`g.A]XhYfa 'Ei]n''

5ggYgga Ybh (. 5gg][ba Ybhg

GhUfhXUhY.Bch5dd`]WUV`Y

8YHJ]`g.5gg][ba Ybhg

5ggYgga Ybh). :]bU`9l Ua

GhUfhXUhY. Bch5dd`]WUV`Y

8YHJ]`g.:]bU``9I Ua

FYgci fWg

DfYgWf]VYX F Ygci fWyg

GiddcfhaUhYf]U`Zcf'h\]g`WcifgY`]bWiX]b[Zk\YbYjYf`UjU]`UV`YžWcd]Yg`cZ`YWifY`bchYgžfYWcaaYbXYX fYUX]b[gžYhW`WUb`VY`ZcibX`cb'AccX`Y"

H\Y`YWMifY`bchY`aUmVY`j]YkYX`UbX`Xckb`cUXYX`Zfca`h\Y`IBGK!AccX`Y` \hnd.##accX`Y`hY`h'ibgk"YXi"Ui#

FYWca a YbXYX⁻FYgci fWYg

: c``ck]b[g'UfY 'h\Y 'fYWVca YbXYX 'Vcc_g'Zcf'h\]g'Wci fgY"

• 8g`VS_WfS'e aXDWeWcha[d7`Y[`WWcq[`Yž'8U_Y'f%+, Ł"

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

H\Y'GW\cc``\Ug'XYjY`cdYX'U'[i]XY`]bY'hc'\Y`d'mci'k\Yb'giVa]hhjb['U'WcifgY'Ugg][baYbh'

K Y`YbWcifU[Y`mci`hc`fYHU]b`U`WcdmcZYjYfmUgg][baYbhgiVa]HYX`Zcf`UggYggaYbhZcf`mcif`ckb`fYWcfX Y]h\Yf`]b`\UfXWcdmcf`Y`YWffcb]WZcfa"

5```UggYgga Ybhg`a i gh\Uj Y`Ub`UggYgga YbhWcj Yf`g\YYhUhUV&YX"

7cifgY'Wcad`Yh]cb

7 ci fgY Wea d`Yhjcb`fYei]fYg`gi Va]gg]cb`cZU```UggYgga Ybh`]hYa g"`: U]`i fY`hc`gi Va]hU```UggYgga Ybh`]hYa g a UmfYgi `h`]b`h\Y`Uk UfX`cZUb`I bgUhjgZUWcfm: U]`i fY`fI : Ł`[fUXY`Zcf`h\Y`7 ci fgY`i b`Ygg`gdYWjU` Webg]XYfUhjcb`\Ug`VYYb`gi Va]hhYX`UbX`Uddfcj YX"`D`YUgY`bchYž'U`Wea dYhYbWm\i fX`Y`cZ) \$i ``]g`Udd`]YX`hc h\Y`ZjbU``UggYgga Ybh'

@UhY Gi Va]gg]cb cZUb 5gg][ba Ybh

: i ```a Uf_g`Zcf`Ub`Ugg][ba YbhUfY`cb`mdcgg]V`Y`k \Yb`Ub`Ugg][ba Ybh`]g`fYWY]j YX`Vmh\Y`Xi Y`XUhY''`

K Y'i bXYfgHUbX'h\Uh'Uh'h]a Yg'mci 'a Umbch'VY'UV'Y'hc'gi Va]h'Ub'Ugg][ba Ybh'cb'h]a Yž'UbX'h\Y'GV\\cc``k]`` UVW&a a cXUhY'UbmZU]f'UbX'fYUgcbUV'Y'YI hYbg]cb"'K Y'k ci `X'fYV&a a YbX'mci 'fYj]Yk 'h\Y'I BGK 'GdYVJU` 7 cbg]XYfUh]cb'[i]XY`]bYg'-gYY'gYWf]cb'VY'ck "

@UhY`gi Va]gg]cb`k]```bchVY`UVWYdhYX`UbX`k]```VY`Wcbg]XYfYX`Ug`bc`gi Va]gg]cb"

GdYWJU``7cbg]XYfUh]cb

- DfYj Ybhimci Zfca 'Wca d'Yhjb['U'Wci fgY'fYei]fYa Ybh
- ? YYd mci 'Zfca 'UHYbX]b['Ub'UggYggUV'Y'UWf]j]m
- Ghcdimci igi Va]hh]b[iUggYggUViYik cf_iZcfiUiWci fgY
- G][b]ZWUbhmUZYWhinci f`dYfZcfa UbW']b`UggYggUV`Y`k cf_žVY`]hU`Zcfa U``YbX!cZgYa YghYf YI Ua]bUh]cbž'U`WUgg`hYghž'U``UVcfUhcfmhYghž'U`gYa]bUf`dfYgYbhUh]cb`cf`Ubmch\Yf`Zcfa `cZ UggYgga Ybh

K Y`Ug_`h\Uhimci `d`YUgY`WcbhUWih\Y`7 ci fgY`7 cbj Ybcf`]a a YX]UhY`mcbWY`mci `\Uj Y`Wca d`YhYX`h\Y`gdYW]U` Wcbg]XYfUh]cb`Udd`]WUh]cbžbc``UhYf`h\Ub`cbY`k YY_`Zca `gi Va]gg]cb"

A VI NYD %oo %oo %oo %oo	Α	A)j	h\Yb	‰	‰	‰	‰	' %	60
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- | BGK `@YUfb]b[`7YblfY`!`<u>k k k "`\\ii bgk "YXi "Ui</u>
- 7 ci bgY``]b['gi ddcfh! '<u>k k k "Wci bgY``]b["i bgk "YXi "Ui</u>

9ei]HUV`Y`@YUfb]b[`GYfj]VW`g`U]a g`hc`dfcj]XY`U```gh`XYbhg`k]h\`U`ZYY`UbX`WcbZ]XYbh]U``gYfj]VW`h\Uh dfcj]XYg`dfUWh]WU``gi ddcfhhc`Ybgi fY`h\Uhmci f`\YU`h\`WcbX]h]cb`XcYgbfhiUXjYfgY`mUZZYWhmci f`gh`X]Yg''` \hhdg.##gh`XYbh'i bgk "YXi "Ui #Y`g

5WUXYa]W<cbYghmUbX D`U[]Uf]ga

Mci f``YWi fYf`UbX`h\Y`I b]j Yfg]mik]``YI dYWinci f`gi Va]hYX`Ugg][ba Ybhg`UfY`hfi `minci f`ck b`k cf_"`I BGK \Ug`j YfmWYUf`[i]XY`]bYg`cb`k \Uhd`U[]Uf]ga `]g`UbX`\ck `hc`Uj c]X`]h'`D`U[]Uf]ga `]g`i g]b[`h\Y`k cfXg`cf]XYUg`cZch\Yfg`UbX`dfYgYbh]b[`h\Ya `Ug`nci f`ck b"`D`U[]Uf]ga `]g`U`mdY`cZ]bhY``YWi U``h\YZh'`+i`WUb`hU_Y a UbmZcfa gž`Zīca `XY`]VYfUhY`W\YUh]b[`hc`UVW]XYbhU``mVcdm]b[`Zīca `U`gci fWY`k]h\ci hUW_bck `YX[Ya Ybh' H\Y`I b]j Yfg]mi\Ug`UXcdhYX`Ub`YXi WUh]j Y`UddfcUV\'hc`d`U[]Uf]ga `UbX`\Ug`XYj Y`cdYX`U`fUb[Y`cZ fYgci fWYg`hc`gi ddcfhigh XYbhg''`5```h\Y`XYhU]`g`cb`d`U[]Uf]ga ž`]bWi X]b[`gca Y`i gYZ ``fYgci fWYgž`WUb`VY Zci bX`Uhi<u>k k k "qh XYbh'i bgk "YXi "Ui #d`U[]Uf]ga</u> "

5```A]b]b[`'9b[]bYYf]b['gh XYbhg`UfY`fYei]fYX`hc`Wcad`YhY`U`gh XYbhXYWUfUh]cb`Zcf`UWUXYa]W]bhY[f]hm k \]WX`]g`ci h]bYX`]b`h\Y`Ugg][baYbhWcj Yf`g\YYhg"`6mg][b]b[``h\]g`XYWUfUh]cbž`mci``U[fYY`h\Uhmci f`k cf_`]g mci f`ck b`cf][]bU``k cf_"

-Zmci 'bYYX'gca Y'UXX]h]cbU``gi ddcfhk]h\ 'mci f`k f]h]b['g_]`gž'd`YUgY'WcbhUWh\Y'@YUfb]b['7 YbhY'cf'j]Yk gca Y'cZh\Y'fYgci fW'g'cb'h\Y]f`k YVg]hY. <u>k k k "`Wi bgk "YXi "Ui</u>"'H\Y'@YUfb]b['7 YbhY']g'XYg][bYX'hc`\Y`d mci ']a dfcj Y'mci f'UWUXYa]Wk f]h]b['UbX'Wca a i b]WUh]cb'g_]``g"'Gca Y'gh XYbhg'i gY'h\Y'7 YbhY'gYfj]WYg VYWUi gY'h\Ym'UfY'Z]bX]b['h\Y]f'Ugg][ba Ybhg'U'W\U``Yb[Yž'ch\Yfg'VYWUi gY'h\Ymk Ubhhc']a dfcj Y'Ub'U'fYUXm gi WWYggZ ``UWUXYa]WdYfZcfa UbWY"

5WUXYa]W=bZcfaUh]cb

7 ci fgY FYgi `hg

: cf^{*}XYHJ]`gʻcbʻI BGK ^{*}UggYgga Ybhdc`]Whž'd`YUgY`j]g]h<u>'k k k "gh XYbh'i bgk "YXi "Ui #UggYgga Ybh</u>

=ðigca Yi]bgHJbWYgimci fiZ]bU``Wci fgYifYgi `ha UmVYik]H\\Y`X`UbX`bchfY`YUgYX`cbiH\Y`I_BGK_id`UbbYX`XUHY" H\]gi]gi]bX]WJHYX`VmU`Wci fgYi[_fUXYifYgi `hicZY]H\Yf.

- @9'-`]bX]WUhYg'mci `\UjY'bchWca d`YhYX'cbY'cf'a cfY']hYa g`cZUggYgga Ybh/cf
- K 8 --]bX]WUhYg'h\YfY']g'Ub']ggi Y'k]h\cbY'cf'a cfY'Ugg][ba Ybh/cf
- K 7 '--'k \]WX ']bX]WUHYg mci '\Uj Y 'Udd`]YX 'Zcf'GdYW]U` '7 cbg]XYfUH]cb'Xi Y 'hc']` bYgg'cf'a]gUXj YbH fY UbX 'h\Y Wci fgY'fYgi 'hg'\Uj Y 'bchVYYb 'Z]bU`]gYX"

=0`Y]h\Yf`YjYbh]hk ci `X`VY`mci f`fYgdcbg]V]`]mhc WebhUWh\Y`7 ci fgY`7 cbjYbYf`Ugʻgccb`UgʻdfUWh]WUV`Y`Vi h bc``UhYf`h\Ub`ZjYf) EXUmg`UZhYf`fY`YUgY`cZh\Y`Wei fgY`fYgi `h''=Zmci `Xcb'hWebhUWh\Y`WebjYbYf`cb`h]a Yž mci `a UmVY`fYei]fYX`hc`fY!gi Va]hUb`Ugg][ba Ybhcf`fY!g]hh\Y`ZjbU``YI Ua `UbX`a UmfYgi `h`]b`mci `ZJ]`]b[`h\Y Wei fgY"'Nci `k ci `X`U`gc`\UjY`U`B 7`fWei fgY`bchWea d`YhYXE'a Uf_`cb`mci f`hfUbgWf]dhUbX`k ci `X`bYYX`hc`fY! Ybfc```]b`h\Y`Wei fgY"

Ghi Xm]b['U'Wci fgY']b'h\Y'GW\cc``cZA]bYfU`g'UbX'9bYf[mFYgci fWfg 9b[]bYYf]b['Uh'I BGK

FYdcfhkf]h]b[[i]XY

H\Y`GW\cc``\Ug`U`<u>FYdcfhK_f]hb[`; i]XY`fFK; Ł</u>`Uj U]`UV`Y"`5`WcdmcZh\]g`]g`Uj U]`UV`Y`cb`h\Y`Wci fgY A ccX`Y`g]hY"

7ca di hjb[FYgci fWrg UbX + bhrfbYh5WWrgg FYei]fYa Ybhg

I BGK 'A]bYfU`gʻUbX`9bYf[mFYgci fWYgʻ9b[]bYYf]b['dfcj]XYgʻV`YbXYX``YUfb]b['i g]b['h\Y`cb!`]bY`A ccX`Y @A G`ff@YUfb]b['A UbU[Ya YbhGmghYa Ł"`5`gc`gYY`! 'HfUbg]h]cb]b['hc`Cb`]bY @YUfb]b[...<u>'k k k "Wcj]X%-ghi Xmcb`]bY"i bgk "YXi "Ui</u>

#i]g'YggYbh]U`'h\Uhmci `\Uj Y'UWWgg'nc'U'D7 'cf'bchYVcc_'Wca di hYf"'A cV]'Y'XYj]Wyg'gi W\'Ug'ga Ufhid\cbYg UbX'HUV'Yhg'a UmWca d`]a Ybh`YUfb]b[ž'Vi hUWWgg'nc'U'D7 'cf'bchYVcc_'Wca di hYf']g'U'gc'fYei]fYX"'BchY h\Uhigca Y'gdYW]U`]ghYb[]bYYf]b['gcZnk UfY']g'bchUj U]'UV'Y'Zcf'A UWWca di hYfg"

- A]b]b['9b[]bYYf]b['Ghi XYbhg. 'CA 6'; (,
- DYhfc`Yi a '9b[]bYYf]b['Ghi XYbhg. H9H6'@, '('/'@, '')

⊨fi]gʻfYWca a YbXYXʻh\Uhimci `\Uj YʻfY[i `Uf`]bhYfbYhUWWYggʻhcʻdUfh]W]dUhY`]bʻZcfi a `X]gW gg]cbʻUbX`[fci d k cf_"`Hc`fi bʻA ccX`Y`a cghYZZYWfj Y`mžmci `g\ci `X`\Uj Y.

5W_bck `YX[Ya YbhcZ7ci bhfm

 $\label{eq:constraint} \begin{array}{l} K_{1}^{*}(UW_{bck}^{*})X_{1}^{*}(V'_{b}Y'_{$